



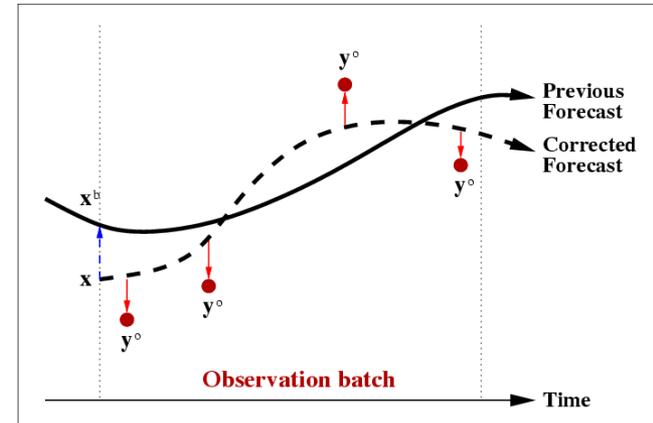
The Met Office hybrid data assimilation scheme

Using ensemble information to improve deterministic forecasts

Adam Clayton, Dale Barker, Neill Bowler, Peter Jermey, Andrew Lorenc, Rick Rawlins, Mike Thurlow
9th Adjoint Workshop, October 2011

Introduction

- Since late 2004, Met Office global data assimilation has been done using 4D-Var:
- **Key question:** How do we specify the “background” error characteristics at the beginning of the window?
- **Traditional approach:** Explicitly model (parameterise) the covariances.
- **Main problem:** Difficult to incorporate to “Errors of the Day”
- **Solution:** Blend in covariance data from an ensemble system, creating a “hybrid” covariance model
- Hybrid system implemented 20th July 2011, coupling to MOGREPS-G ensemble system
- Increasing synergy between ensemble forecasting and data assimilation





Outline of talk

- Climatological vs. ensemble covariances
- Hybrid VAR formulation
- Pre-operational trials, and verification
- Plans

(History)

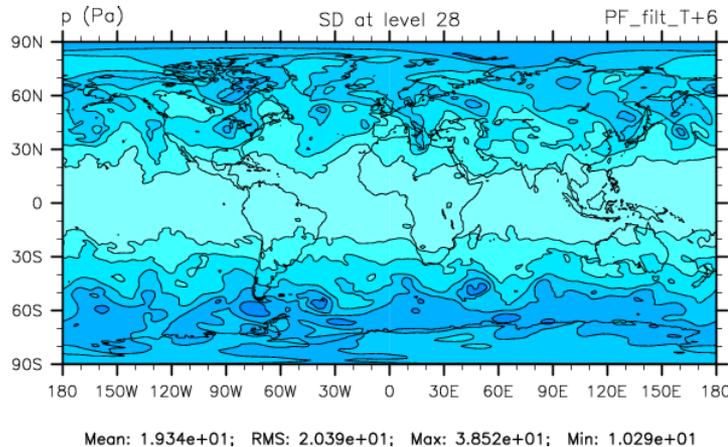
(References)

Climatological covariances (B_C)

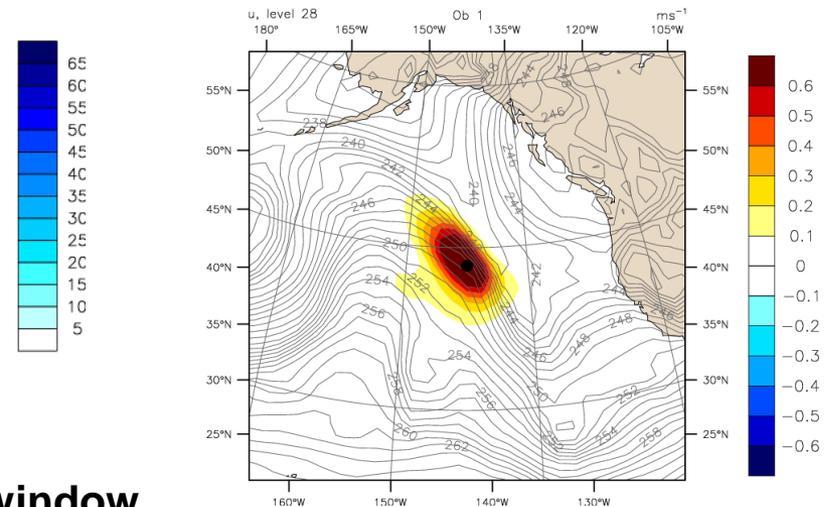
- Until July 2011, 4D-Var was based wholly on climatological covariances:
 - Choose control variable fields that are approximately uncorrelated:

ψ : streamfunction	χ : velocity potential
A_p : Unbalanced pressure	μ : humidity
 - Assume their covariances are horizontally isotropic and zonally uniform.
 - Get parameters from training data. (Currently, the ECMWF 4D-Var ensemble)

SD (pressure)



Pseudo ob test (u)



End of window

Ensemble covariances (P_e)

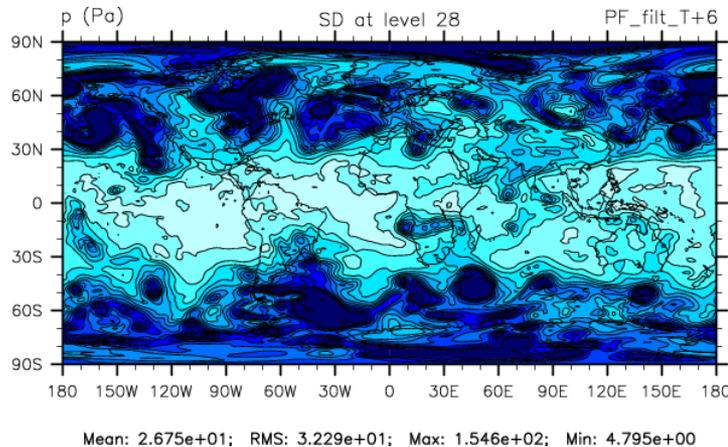
- MOGREPS-G:

- 23 perturbed members (N216L70), aimed at the short-range
- Ensemble covariance is a simple outer product of the forecast perturbations:

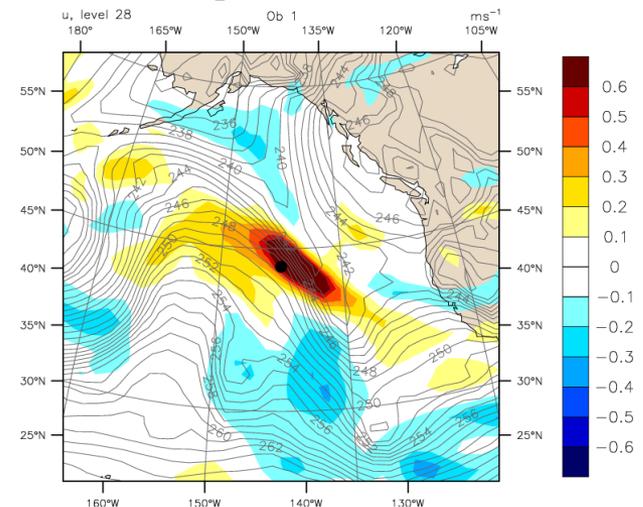
$$P_e = XX^T; \quad X = \frac{1}{\sqrt{K-1}}(x_1 - \bar{x}, x_2 - \bar{x}, \dots, x_K - \bar{x})$$

- Provides covariances that should reflect the observation distribution, and the effects of recent instabilities; i.e., the “Errors of the Day”

SD (pressure)



Pseudo ob test (u)



End of window

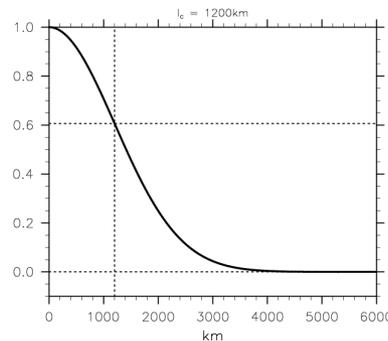
The need to localise P_e

- Ensemble covariances are noisy. In particular, there are spurious long-range correlations:
- Solution is to “localise” the covariances, by multiplying pointwise with a localising covariance C_{loc} :

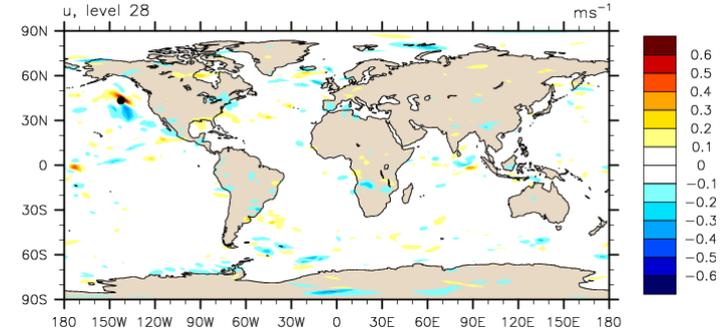
$$P_e \rightarrow P_e \circ C_{loc}$$

(Lorenc 2003)

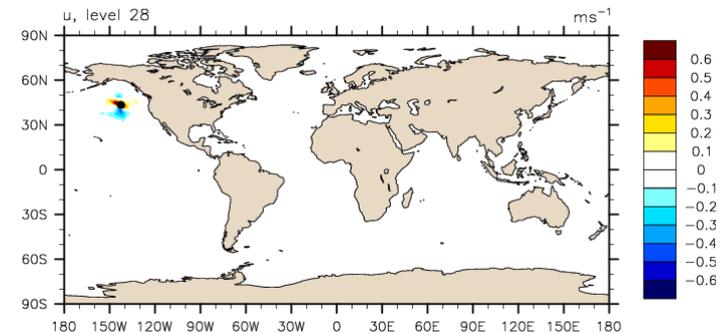
$$P_e \circ$$



$$P_e \rightarrow$$



$$\rightarrow$$



- Crucially, localisation also increases the “rank” of the ensemble covariances: the number of independent structures available to fit the observations.
- (No localisation implies just 23 global structures!)



Hybrid covariances

- In summary, we have two approaches to modelling \mathbf{B} (there is a 3rd):
 - \mathbf{B}_c : Traditional climatological covariance
 - **Full-rank, but heavily modelled/parametrised, and insensitive to "Errors of the Day"**
 - $\mathbf{P}_e \circ \mathbf{C}_{loc}$: Localised ensemble covariance
 - **Reflect errors of the day, but relatively low-rank, and may be damaged by the need to localise**
- Which is better?
 - Depends on the ensemble size/quality, and how well $\mathbf{B}_c/\mathbf{C}_{loc}$ are modelled
 - Buehner et al. 2010 showed they're competitive. (96-member EnKF provided the modes)
 - **But** e.g. Wang et al 2008 show that a hybrid is better:

$$\mathbf{B} = \beta_c^2 \mathbf{B}_c + \beta_e^2 \mathbf{P}_e \circ \mathbf{C}_{loc}$$

- (Hybrid also provides a smooth path to fuller use of $\mathbf{P}_e \circ \mathbf{C}_{loc}$ as ensemble size increases)



Hybrid VAR formulation

- Basic code written in late 90's! (Barker and Lorenc)
- VAR with climatological covariance \mathbf{B}_c :

$$\mathbf{B}_c = \mathbf{U}\mathbf{U}^T \quad \delta\mathbf{w}_c = \mathbf{U}\mathbf{v} = \mathbf{U}_p\mathbf{U}_v\mathbf{U}_h\mathbf{v}$$

- VAR with localised ensemble covariance $\mathbf{P}_e \circ \mathbf{C}_{loc}$:

$$\mathbf{C}_{loc} = \mathbf{U}^\alpha\mathbf{U}^{\alpha T} \quad \boldsymbol{\alpha}_i = \mathbf{U}^\alpha\mathbf{v}_i^\alpha \quad \delta\mathbf{w}_e = \frac{1}{\sqrt{K-1}} \sum_{i=1}^K (\mathbf{x}_i - \bar{\mathbf{x}}) \circ \boldsymbol{\alpha}_i$$

- **Note:** We are now modelling \mathbf{C}_{loc} rather than the full covariance \mathbf{B}_c .
- Hybrid VAR:

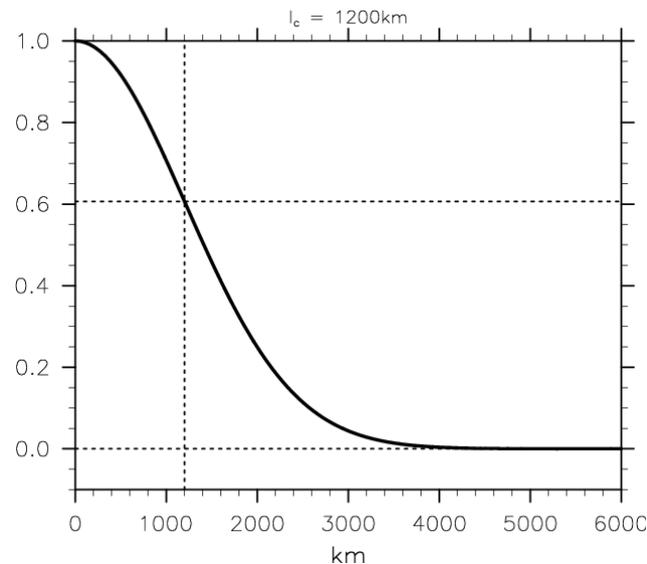
$$\delta\mathbf{w} = \underline{\beta_c} \delta\mathbf{w}_c + \underline{\beta_e} \delta\mathbf{w}_e \quad J = \frac{1}{2} \mathbf{v}^T \mathbf{v} + \frac{1}{2} \mathbf{v}^{\alpha T} \mathbf{v}^\alpha + J_o + J_c$$

Design of localisation

- Localisation performed in control variable space ($\psi, \chi, A\mathbf{p}, \mu$) to help preserve balances.
- Localisation then separated into horizontal and vertical parts:

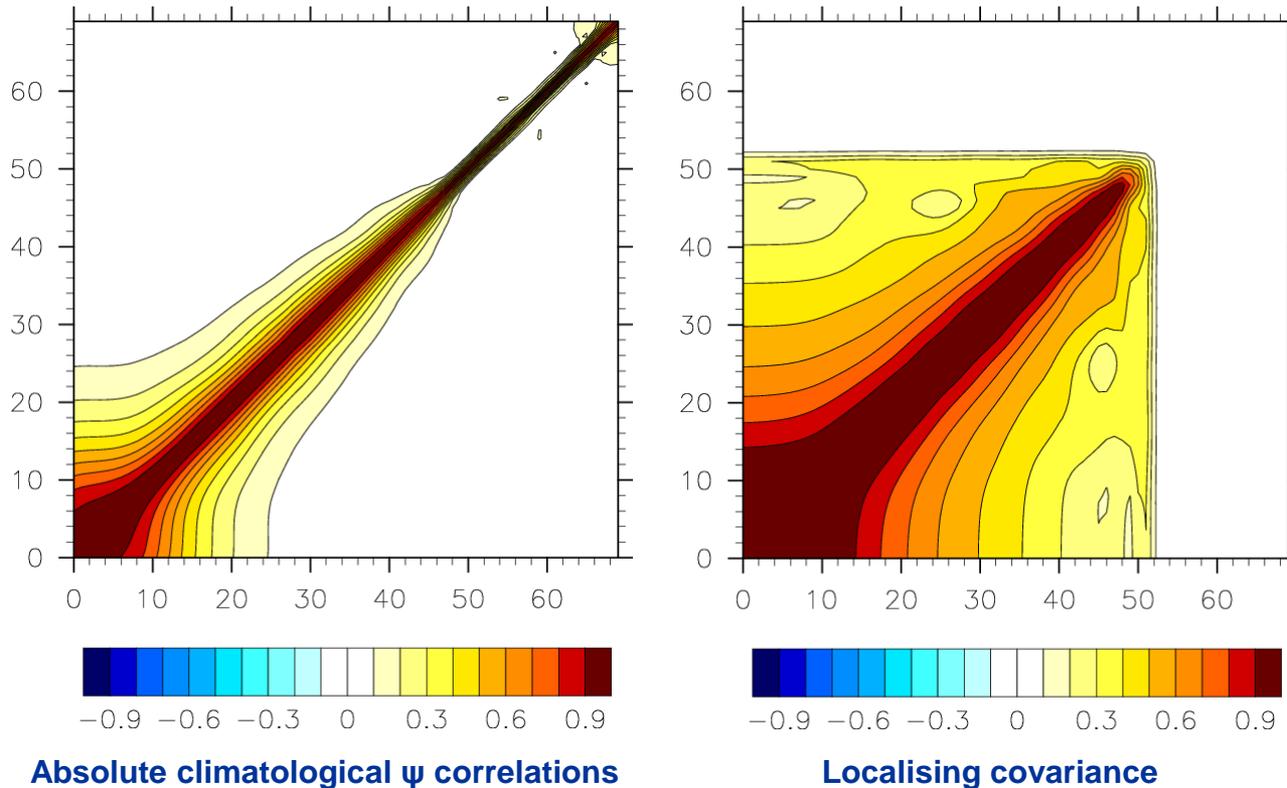
$$\mathbf{U}^{\alpha} = \mathbf{U}_v^{\alpha} \mathbf{U}_h^{\alpha}$$

- Horizontal part a simple (Gaussian) function of separation:



Design of localisation

- Vertical localisation obtained by modifying the streamfunction correlations from \mathbf{B}_c :

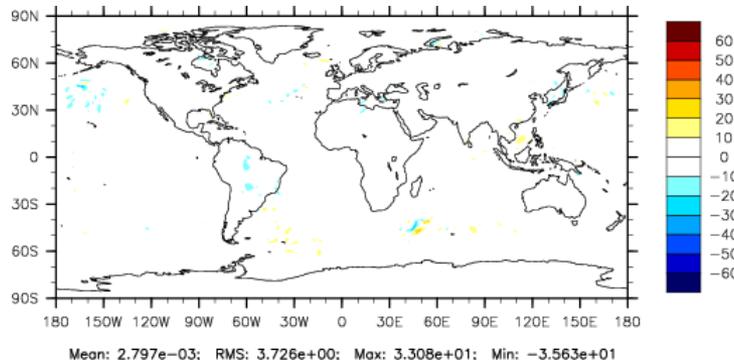


- Ensemble covariance removed above 21 km (~ level 54), for safety!

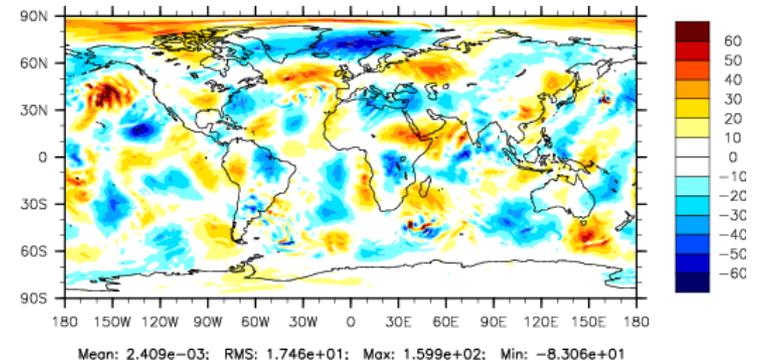
High-pass “anti-aliasing” filter

- MOGREPS modes are well-balanced on entry to VAR, but horizontal localisation causes problems:

p1 time-filter increment (Pa): without localisation

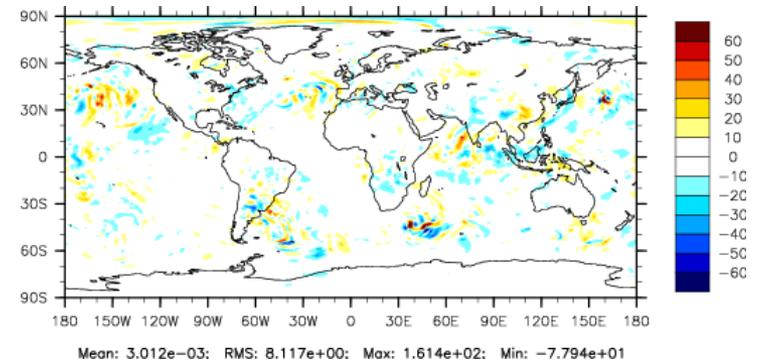


with localisation



- **Why?** Larger scales in the error modes alias onto the localisation scales.
- **Solution:** Apply a high-pass “anti-aliasing” filter to the error modes to downweight larger scales.
- This has the desired effect:

with localisation and high-pass filtering

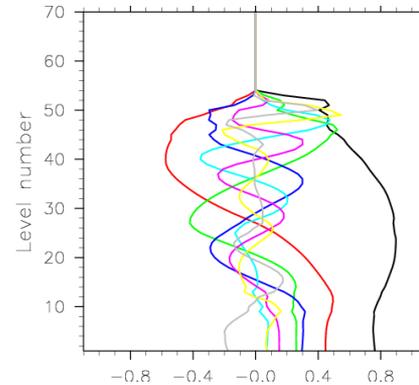


Smoothing of vertical modes

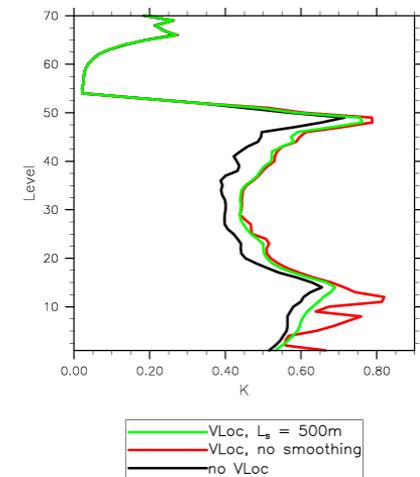
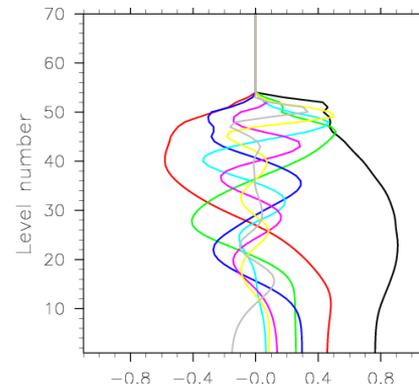
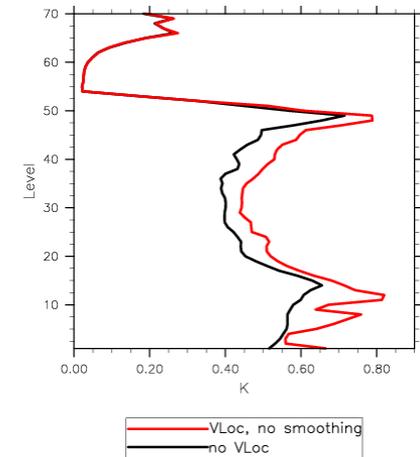
- Original set of vertical modes gave spurious temperature increments near the surface:

- Smoothing the modes largely removes the problem:

Vertical modes

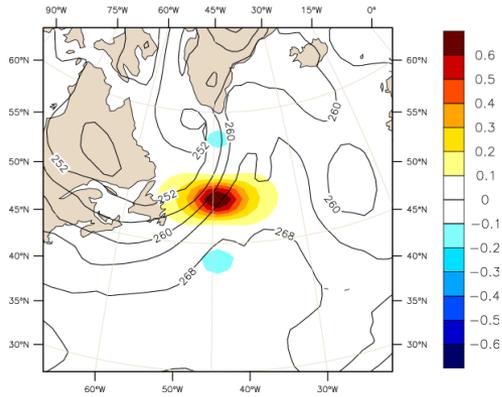


Implied temperature SD

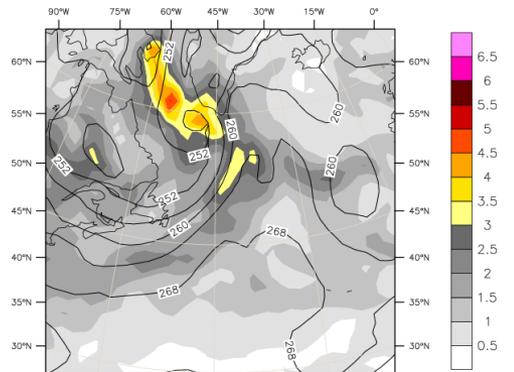


Single observation tests

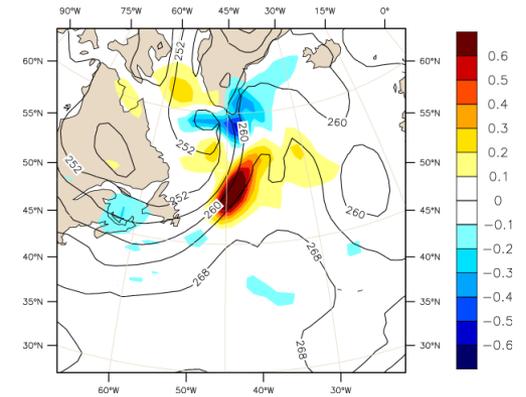
u response to a single u observation at centre of window



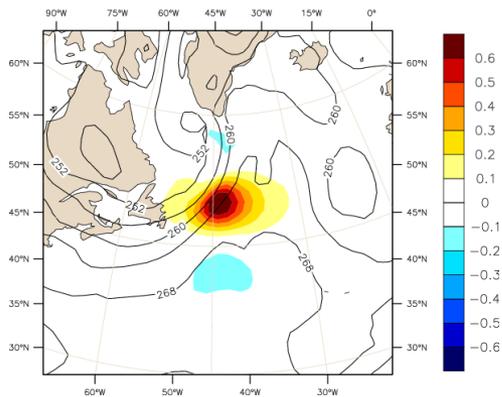
Standard 3D-Var



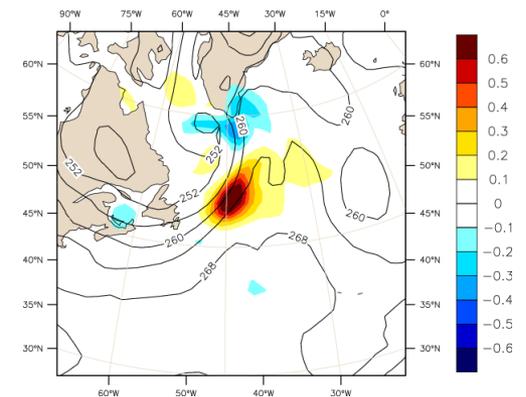
Ensemble RMS



Pure ensemble 3D-Var



Standard 4D-Var

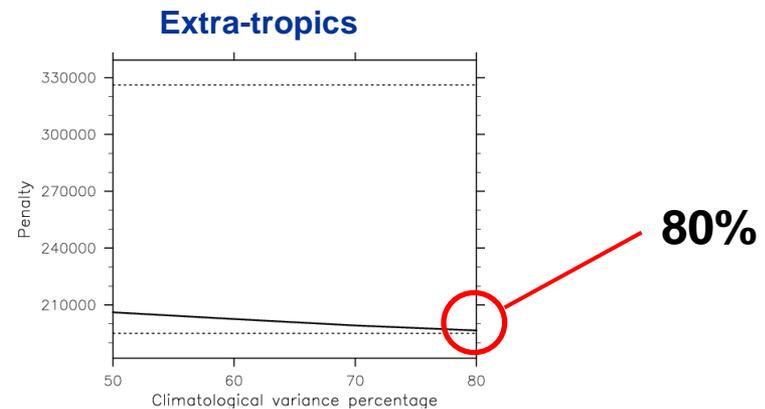
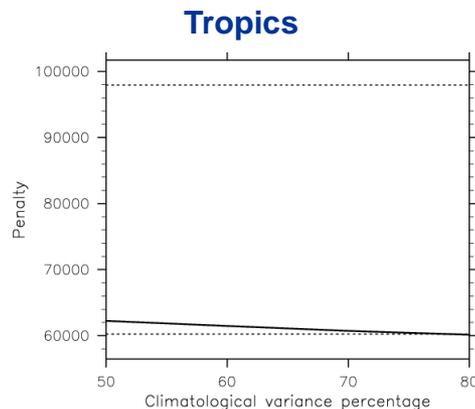


50/50 hybrid 3D-Var



Tuning of climatological / ensemble COV percentages

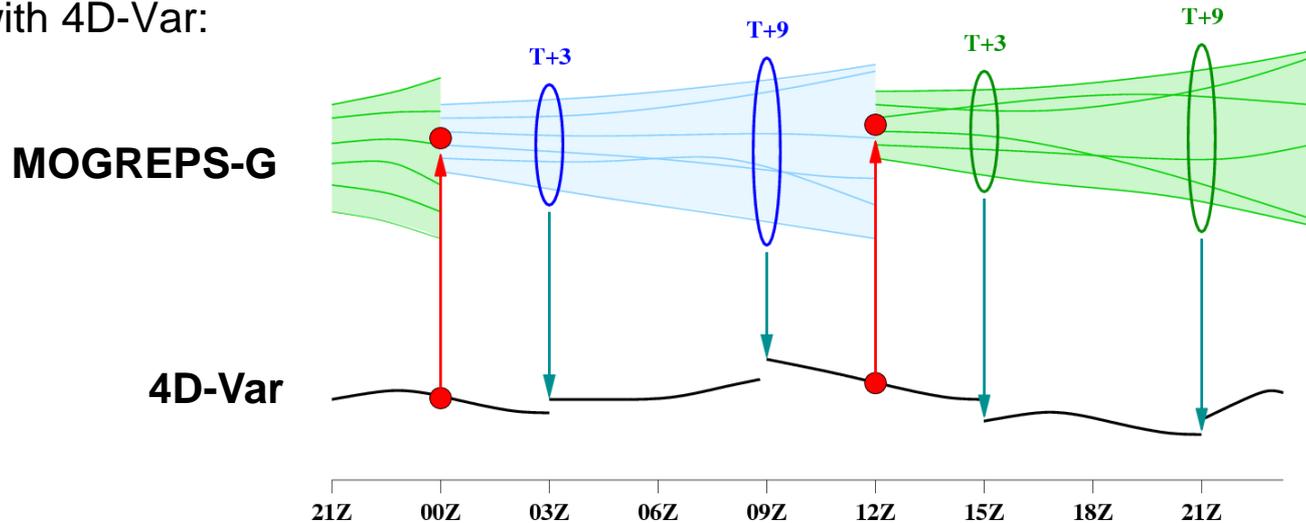
- Low-rank of ensemble covariances means that the available variance is not fully utilised in the analysis.
- 50%-50% climatological/ensemble usage gives final observation penalties ~8-9% higher in both 3D-Var and 4D-Var.
- **Tuning strategy:** Use 50% ensemble covariance, and inflate climatological covariance to preserve analysis fit to obs
- Final observation penalty as a function of climatological percentage, with ensemble covariance usage fixed at 50%:



(..... : Initial and final penalties from control analysis)

Coupling to MOGREPS

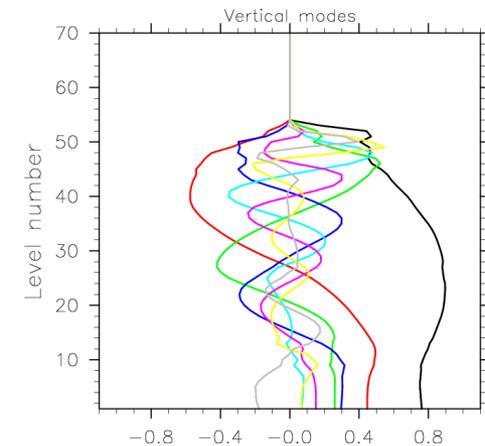
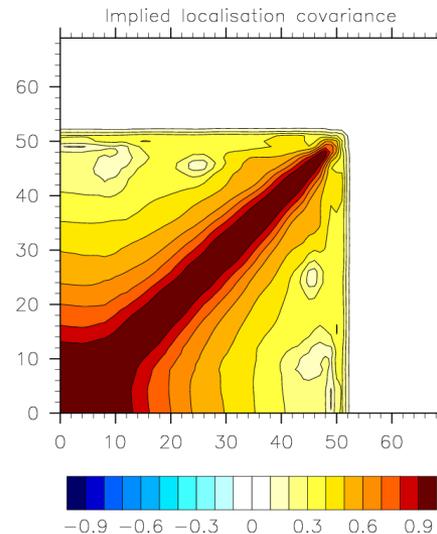
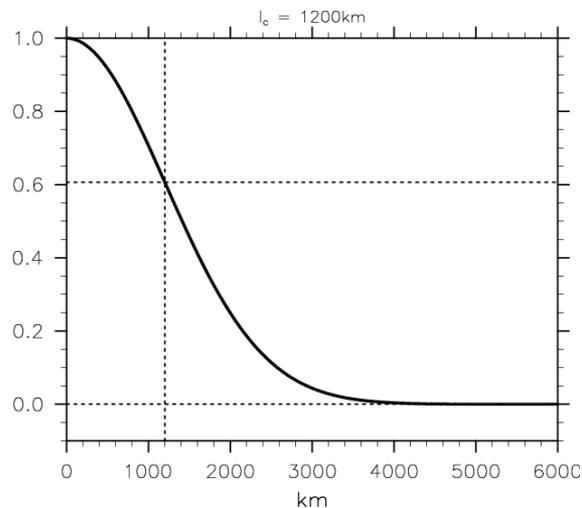
- MOGREPS-G:
 - 23 perturbed members + one control member
 - 12-hour cycle, recentring around deterministic 4D-Var analysis (●)
- Coupling with 4D-Var:



- Pre-hybrid: **4D-Var** → **MOGREPS**
- Post-hybrid: **4D-Var** ↔ **MOGREPS**
- **Note:** 00Z and 12Z analyses use T+9 error modes, with the “wrong” analysis time.

Pre-operational hybrid trials

- Two periods: Dec09/Jan10 (29 days, uncoupled); Jun10 (28 days, coupled + uncoupled)
- **Forecast model:** N320L70: ~40km, 70 levels
- **MOGREPS-G:** N216L70: ~60km. 23 perturbed members
- **VAR:** N108L70/N216L70: ~120km→~60km.
- Horizontal localisation scale $L_c = 1200\text{km}$. (The distance at which the correlation reaches $e^{-1/2}$)
- Relaxation to standard climatological covariances between 16 and 21km
- **Note:** Trials run without smoothing of vertical modes (to remove spurious T variances)





Pre-operational hybrid trials

Verification vs. obs

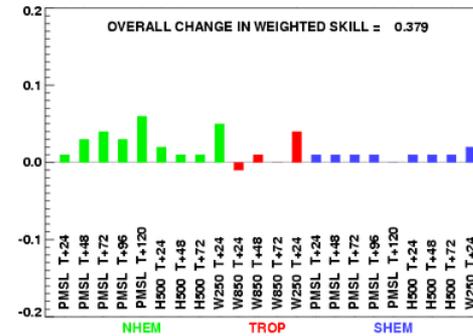
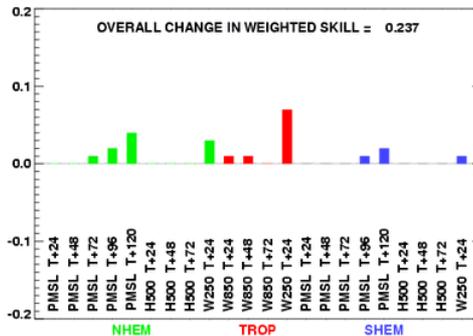
Better/neutral/worse

	NH	TR	SH
Dec uncoupled (29 days)	29/94/0	6/117/0	12/109/2
Jun coupled (28 days)	34/89/0	9/114/0	46/74/3

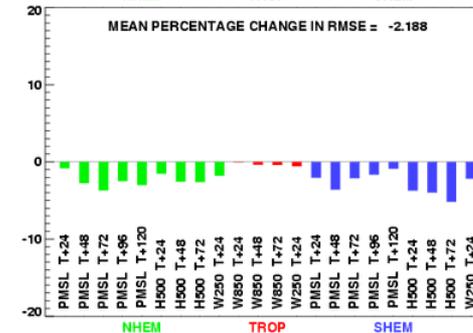
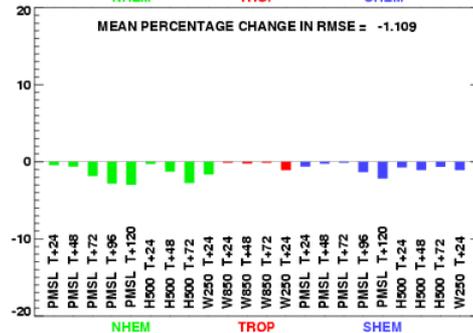
Dec uncoupled: 1.211 (0.874%)

Jun coupled: 1.587 (1.226%)

Skill:



RMSE:

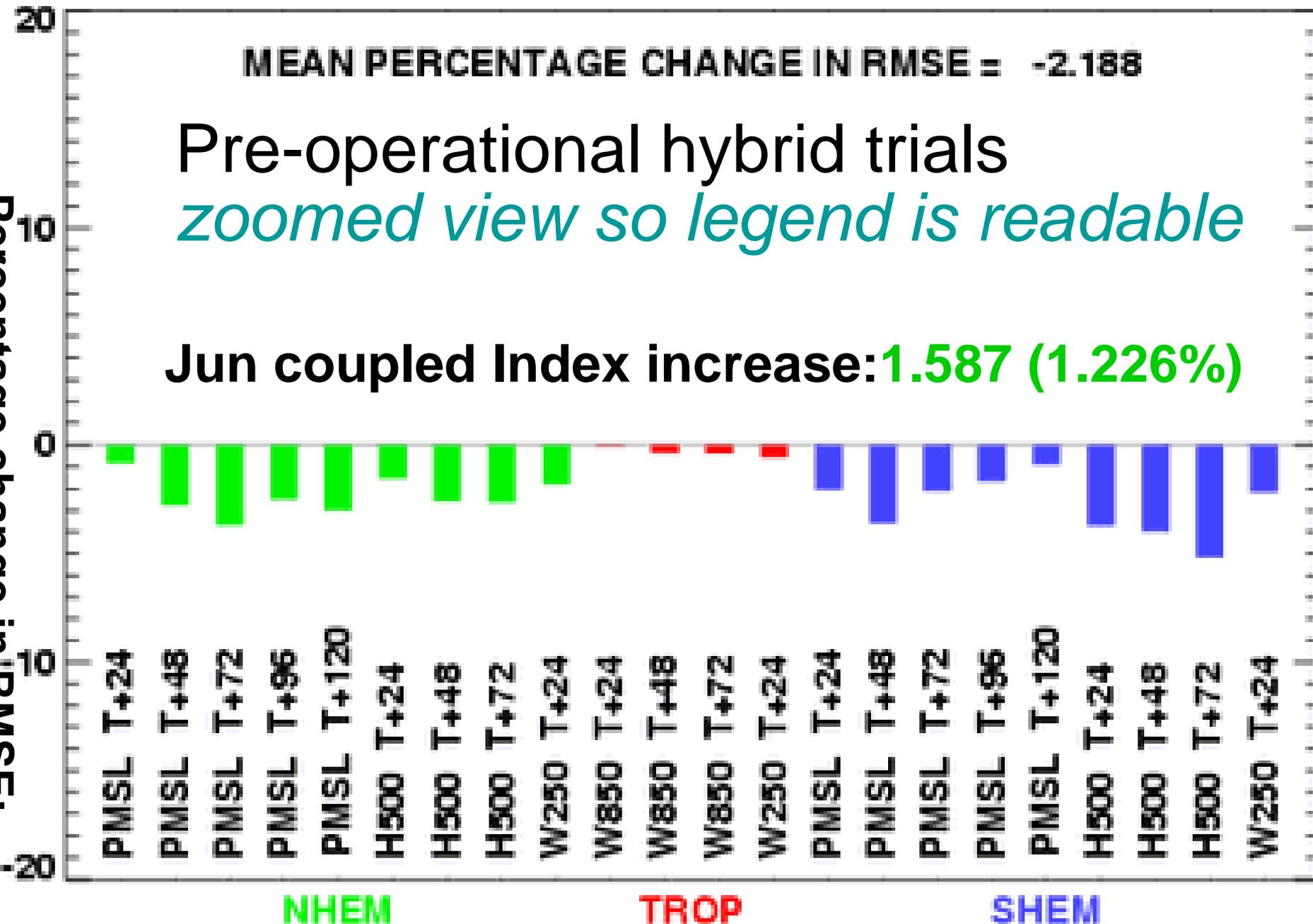


MEAN PERCENTAGE CHANGE IN RMSE = -2.188

Pre-operational hybrid trials
zoomed view so legend is readable

Jun coupled Index increase: 1.587 (1.226%)

Percentage change in RMSE:





Pre-operational hybrid trials

Verification vs. own analyses

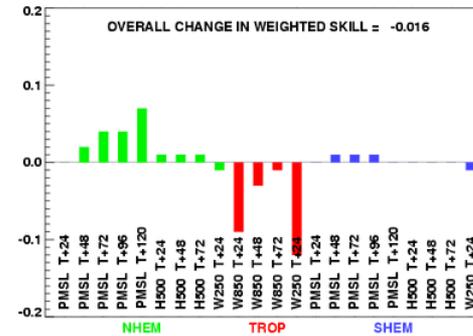
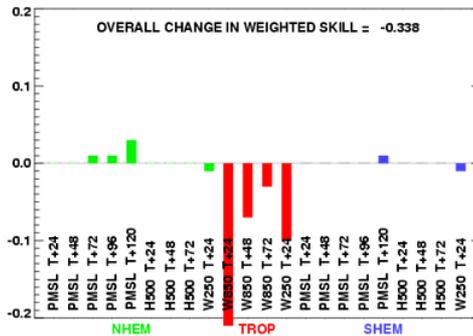
Better/neutral/worse

	NH	TR	SH
Dec uncoupled (29 days)	16/91/16	7/69/47	3/106/14
Jun coupled (28 days)	49/63/11	9/86/28	18/82/23

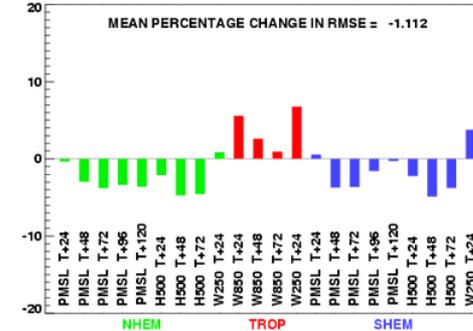
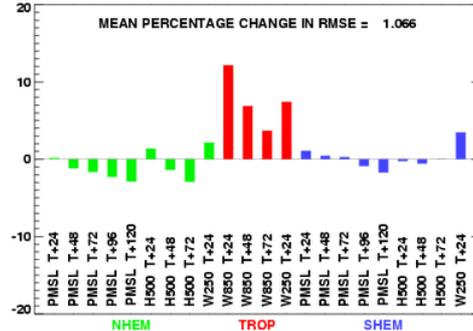
Dec uncoupled: **-3.972 (-2.415%)**

Jun coupled: **-0.151 (-0.100%)**

Skill:



RMSE:





Pre-operational hybrid trials

Verification vs. ECMWF analyses

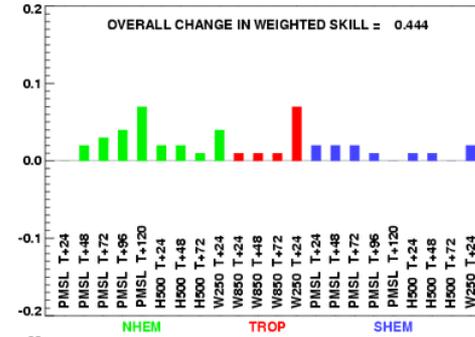
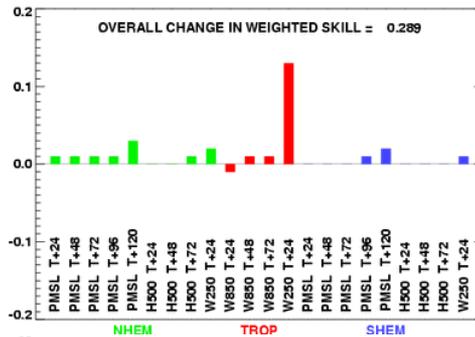
Better/neutral/worse

	NH	TR	SH
Dec uncoupled (29 days)	35/79/0	39/75/0	14/100/0
Jun coupled (28 days)	63/51/0	29/85/0	47/65/2

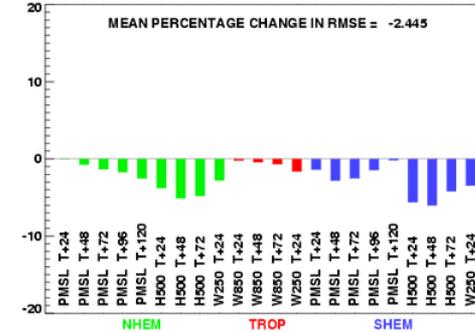
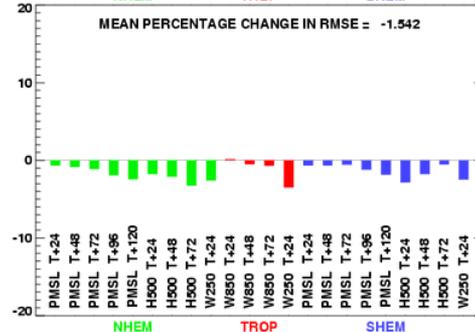
Dec uncoupled: 1.721 (1.338%)

Jun coupled: 1.311 (1.287%)

Skill:



RMSE:



Pre-operational hybrid trials

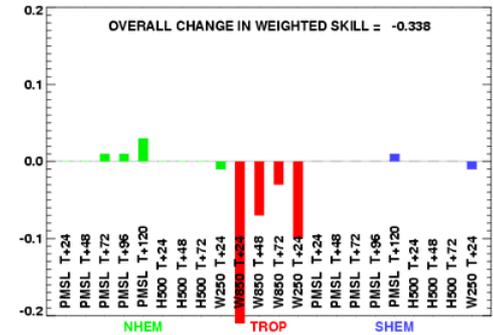
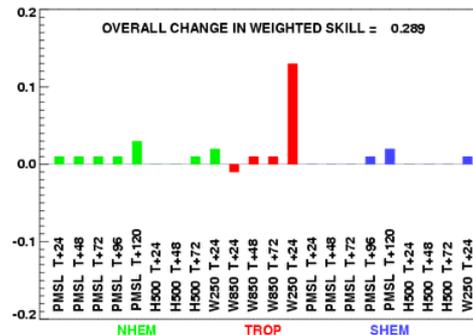
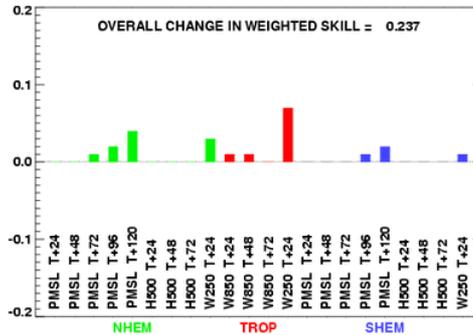
Summary of skill scores

vs. obs

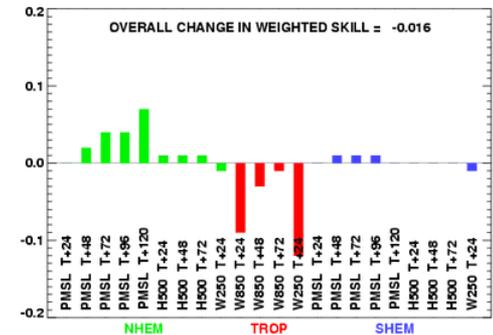
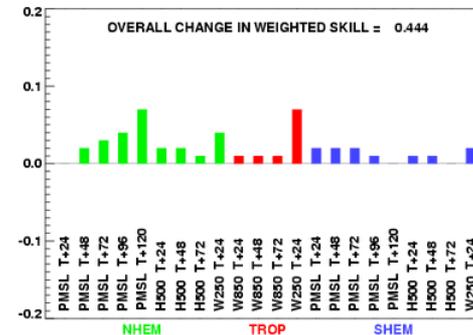
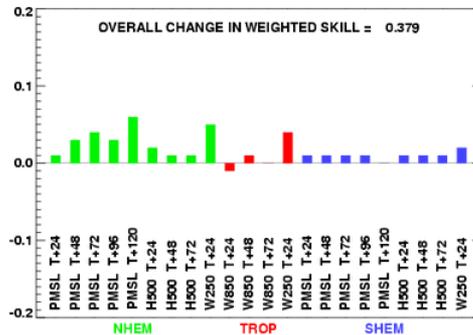
vs. ECMWF analyses

vs. own analyses

Dec uncoupled:



Jun coupled:

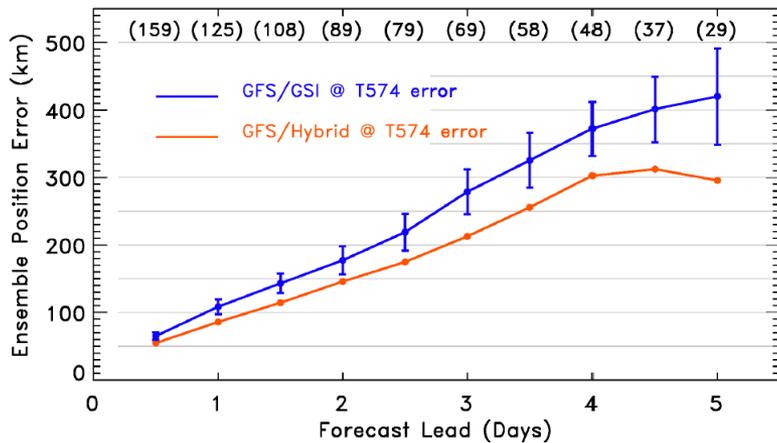


- Scores vs. ECMWF analyses more consistent with scores vs. obs
- When changing the character of the analysis, verification against own analyses is incestuous and misleading, so we are looking to change the NWP index
- (WMO CBS scores will remain flawed!)

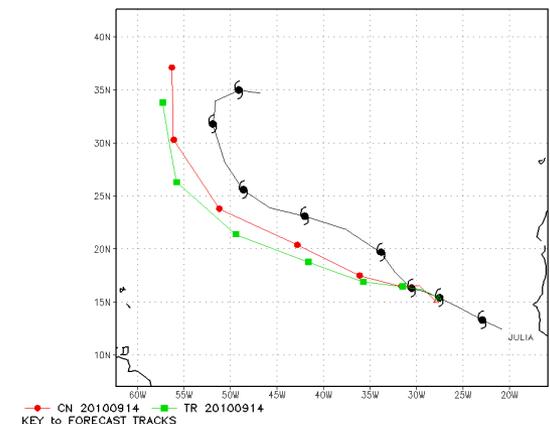
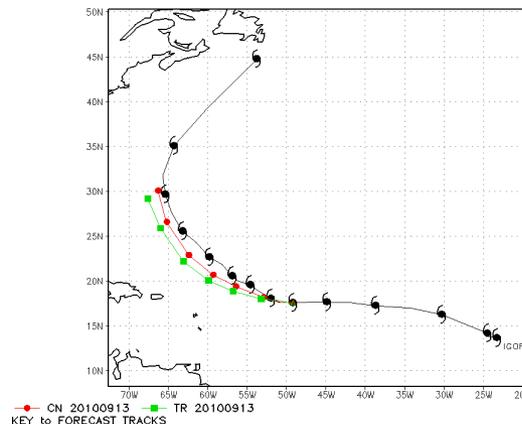
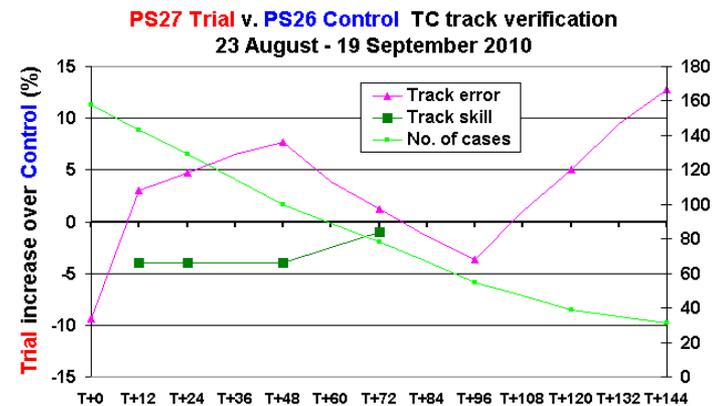
Effect on tropical cyclones (Julian Heming)

- TC track error much improved in GSI 3D-Var hybrid (80 ensemble members):

- If anything, our hybrid makes track errors worse:



(Jeff Whitaker)



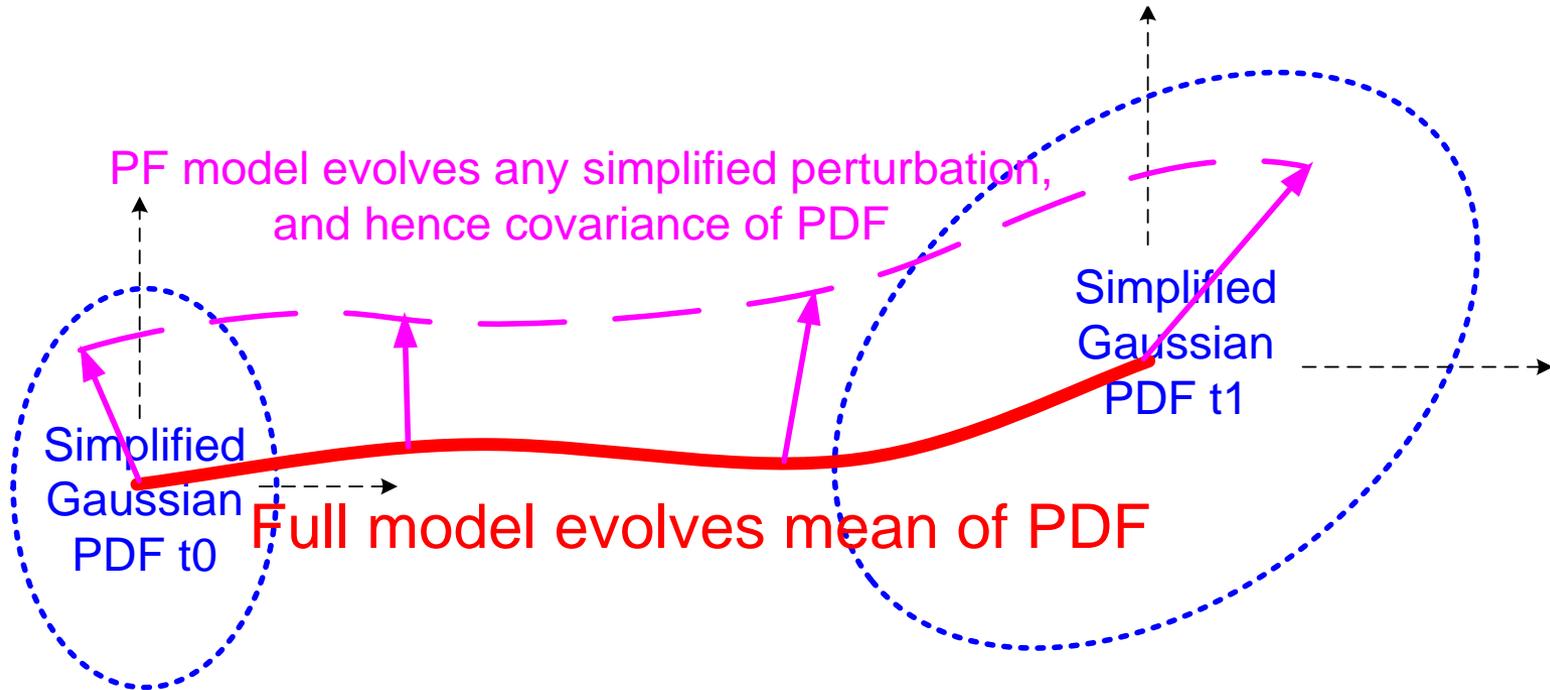


Plans

Met Office

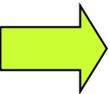
- Publish paper.
- Ensemble (MOGREPS-G) changes:
 - Move to 6-hour cycling.
 - Increase horizontal resolution
 - Increase ensemble size.
- Hybrid development:
 - Waveband localisation (Buehner 2011)
 - Investigate reasons for disappointing TC performance
 - Improve vertical localisation's effect on balance
 - Better understanding of optimal localisation scales
- Possible Limited-Area version
- 4D-Ensemble-Var.

Statistical, incremental 4D-Var



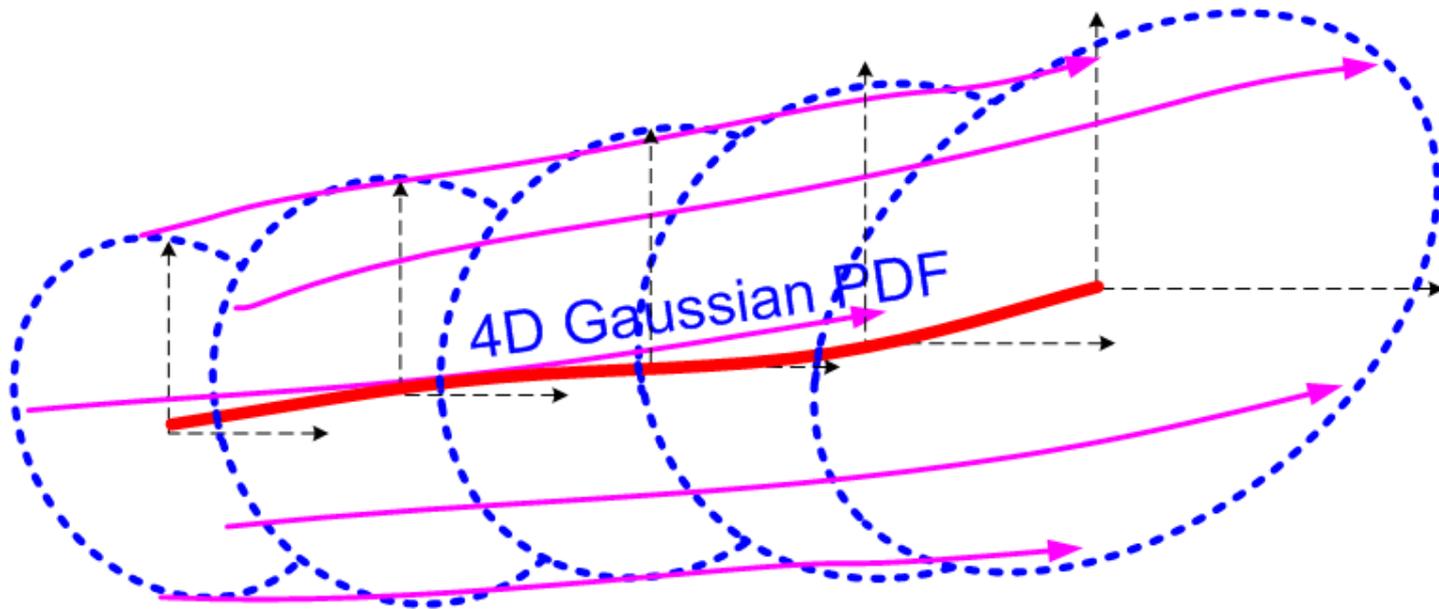
Statistical 4D-Var approximates entire PDF by a Gaussian.

4D analysis increment is a trajectory of the PF model, optionally augmented by a model error correction term.





Incremental 4D-Ensemble-Var

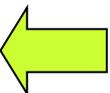


Trajectories of perturbations from ensemble mean

Full model evolves mean of PDF

Localised trajectories define 4D PDF of possible increments

4D analysis is a (localised) linear combination of nonlinear trajectories. It is not itself a trajectory.





4D-En-Var - equations

Analysis variables are the localisation fields $\underline{\alpha}_i$ multiplying each perturbation trajectory $\underline{\mathbf{x}}'_i$ to make the increment trajectory:

Lorenc (2003b), Liu *et al.* (2008), Buehner *et al.* (2010)

The increment trajectory plus the guess are interpolated to the obs:

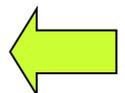
$$\delta \underline{\mathbf{x}} = \sum \underline{\alpha}_i \circ \underline{\mathbf{x}}'_i$$

$$\underline{\mathbf{y}} = \underline{\mathbf{H}} \delta \underline{\mathbf{x}} + \underline{H} \left(\underline{M} \left(\mathbf{x}^g, \underline{\boldsymbol{\eta}}^g \right) \right)$$

The penalty function is more akin to 3D-Var than 4D-Var:

We use standard transforms to model the spatial correlations in \mathbf{C}

$$J(\underline{\boldsymbol{\alpha}}) = \sum \frac{1}{2} \underline{\boldsymbol{\alpha}}_i^T \underline{\mathbf{C}}^{-1} \underline{\boldsymbol{\alpha}}_i + \frac{1}{2} \left(\underline{\mathbf{y}} - \underline{\mathbf{y}}^o \right)^T \underline{\mathbf{R}}^{-1} \left(\underline{\mathbf{y}} - \underline{\mathbf{y}}^o \right)$$





Benefit of outer-loop

- The outer-loop is normally justified as a re-linearisation of a non-quadratic minimisation.
- It can also be thought of as a way of correcting for an imperfect Perturbation model, by reducing the amplitude of the perturbations whose trajectory is approximated:

$$\underline{\mathbf{y}} = \underline{\tilde{\mathbf{H}}}\underline{\tilde{\mathbf{M}}}\left(\underline{\delta\mathbf{x}}, \underline{\boldsymbol{\eta}}\right) + \underline{\bar{H}}\left(\underline{\bar{M}}\left(\underline{\mathbf{x}}^g, \underline{\boldsymbol{\eta}}^g\right)\right)$$

- Of course, with an imperfect perturbation model, there is no guarantee that an outer-loop will converge.



Thanks for listening



History of hybrid at Met Office

(based on Lorenc 2007)

- 1990s: Dale Barker works on EOTD as part of Andrew Lorenc's VAR team. α control variable method developed. The idea was a development of Kalnay and Toth (1994).
- Tests using "Bred Modes" (Adrian Semple 2001, 2003) encouraging, but ensemble (1 perturbation) too small! EOTD project suspended pending an operational Met Office ensemble. (Dale continues research at NCAR.)
- While reviewing EnKF methods, Andrew Lorenc realised that the α control variable method was precisely equivalent to covariance localisation (Lorenc 2003).
- 2008: Project restarted by Andrew Lorenc, Dale Barker & Adam Clayton.
- 2009: 1st version (no vertical localisation) improves 3D-Var but neutral with 4D-Var.
- 2011: Improved version (as described here) implemented.



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